

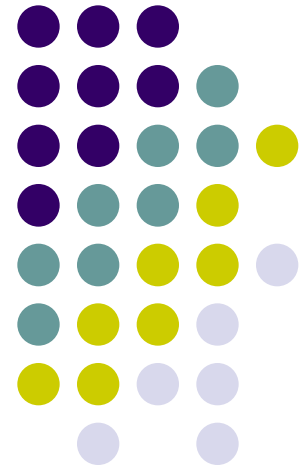
# CS 460

Programming Languages

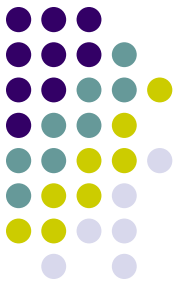
Fall 2021

Dr. Watts

(23 October 2023)



# Assignments

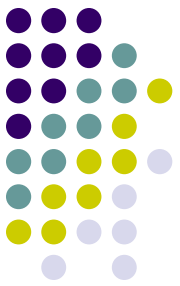


- Project 1
  - Submission script closed
  - New results sent this morning
- Exercise 2
  - Script running so that your groups can improve their testing techniques
- Exercise 3
  - Posted – let me know if you see typos
  - Part 1 due next week
- Project 2
  - Coming soon



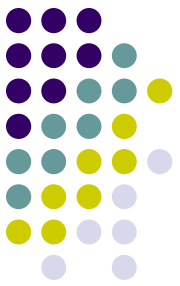
# What is Syntactic Analysis?

- Also known as Parsing
- Determining if the order of the tokens generated for the lexemes of the input are in a legal order according to some grammar
- Creation of a parse tree
  - Explicit or implicit
- Error recovery
  - When an error is detected, the parser must get back to a normal state and continue analysis of the input
- Basis for translation



# VS Semantic Analysis

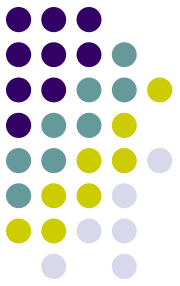
- The meaning of the expressions, statements and program units.
- Static semantics
  - At compile time
- Dynamic semantics
  - At run time
- Attribute grammars
- Denotational semantics



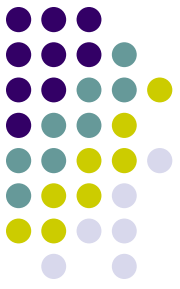
# Describing Syntax

- Language is a set of strings of characters from some alphabet.
- The strings of a language are called sentences or statements.
- Smallest units of the statements are words or lexemes.
- Syntax rules of a language describe what words are in the language and how they should be ordered.
- Natural languages (such as English) have a complex and extensive set of syntactical rules.
- Programming languages have a relatively simple set of syntactical rules.

# BNF



- Set of terminal symbols ( $T$ )
- Set of non-terminal symbols ( $N$ )
- Start symbol ( $S \in N$ )
- Set of production rules ( $P$ )
  - $\langle \text{non-terminal} \rangle \rightarrow$  string of terminal and  $\langle \text{non-terminal} \rangle$  symbols
  - $\langle \text{non-terminal} \rangle ::=$  string of terminal and  $\langle \text{non-terminal} \rangle$  symbols



# Simple BNF Grammar

- $T = \{\text{ONE}, \text{TWO}, \text{THREE}, \text{FOUR}\}$
- $NT = \{\langle \text{number} \rangle, \langle \text{single} \rangle, \langle \text{double} \rangle, \langle \text{triple} \rangle\}$
- $S = \langle \text{number} \rangle$
- $P = \{$ 
  - $\langle \text{number} \rangle ::= \langle \text{single} \rangle \langle \text{double} \rangle \langle \text{triple} \rangle$
  - $\langle \text{single} \rangle ::= \text{ONE} \mid \text{TWO} \mid \text{THREE} \mid \text{FOUR}$
  - $\langle \text{double} \rangle ::= \langle \text{single} \rangle \langle \text{single} \rangle$
  - $\langle \text{triple} \rangle ::= \langle \text{single} \rangle \langle \text{double} \rangle$
  - $\langle \text{triple} \rangle ::= \langle \text{double} \rangle \langle \text{single} \rangle$ $\}$

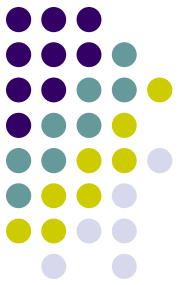
# Taunt Generator Grammar

(with thanks to Monty Python and the Insulting Frenchman)



```
< taunt > ::= < sentence > | < taunt > < sentence > | < noun >!
< sentence > ::= < past-rel > < noun-phrase >
                | < present-rel > < noun-phrase >
                | < past-rel > < article > < noun >
< noun-phrase > ::= < article > < modified-noun >
< modified-noun > ::= < noun > | < modifier > < noun >
< modifier > ::= < adjective > | < adverb > < adjective >
< present-rel > ::= your < present-person > < present-verb >
< past-rel > ::= your < past-person > < past-verb >
< present-person > ::= steed | king | first-born
< past-person > ::= mother | father | grandmother | grandfather | godfather
< noun > ::= hamster | coconut | duck | newt | peril | chicken | vole | parrot
            | mouse | twit | elderberry
< present-verb > ::= is | "masquerades as"
< past-verb > ::= was | personified | "smelt of"
< article > ::= a
< adjective > ::= silly | wicked | sordid | naughty | repulsive | malodorous
                | ill-tempered
< adverb > ::= conspicuously | categorically | positively | cruelly
            | incontrovertibly
```





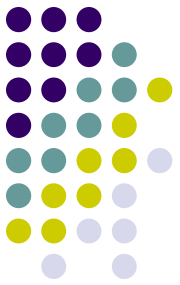
# Each team

- Use the grammar to generate 3 taunts
  - $\leq 5$  words
  - $> 5$  and  $\leq 10$  words
  - $> 10$  words
- Submit the taunts in a file called Team#.txt

# Context Free Grammars and Backus-Naur Form



- Context Free Grammar (CFG) – order of syntactical elements is important – meaning is not.
- Meaning is determined by context semantics.
- Backus-Naur Form (BNF)
  - ALGOL 58
  - John Backus – 1959
  - Peter Naur – 1960
- BNF is a natural notation for describing syntax



# BNF Grammar (Example 1)

- $T = \{=, A, B, C, +, *, (, )\}$
- $N = \{\langle\text{assign}\rangle, \langle\text{id}\rangle, \langle\text{expr}\rangle\}$
- $S = \langle\text{assign}\rangle$
- $P = \{$

$\langle\text{assign}\rangle \rightarrow \langle\text{id}\rangle = \langle\text{expr}\rangle$

$\langle\text{id}\rangle \rightarrow A \mid B \mid C$

$\langle\text{expr}\rangle \rightarrow \langle\text{id}\rangle + \langle\text{expr}\rangle$

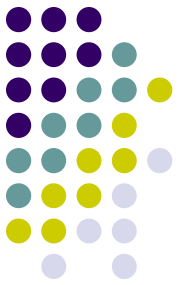
$\mid \langle\text{id}\rangle * \langle\text{expr}\rangle$

$\mid ( \langle\text{expr}\rangle )$

$\mid \langle\text{id}\rangle$

$\}$

# Derivation of $A = B + (C * A)$



<assign>

$\Rightarrow \langle \text{id} \rangle = \langle \text{expr} \rangle$

$\Rightarrow A = \langle \text{expr} \rangle$

$\Rightarrow A = \langle \text{id} \rangle + \langle \text{expr} \rangle$

$\Rightarrow A = B + \langle \text{expr} \rangle$

$\Rightarrow A = B + ( \langle \text{expr} \rangle )$

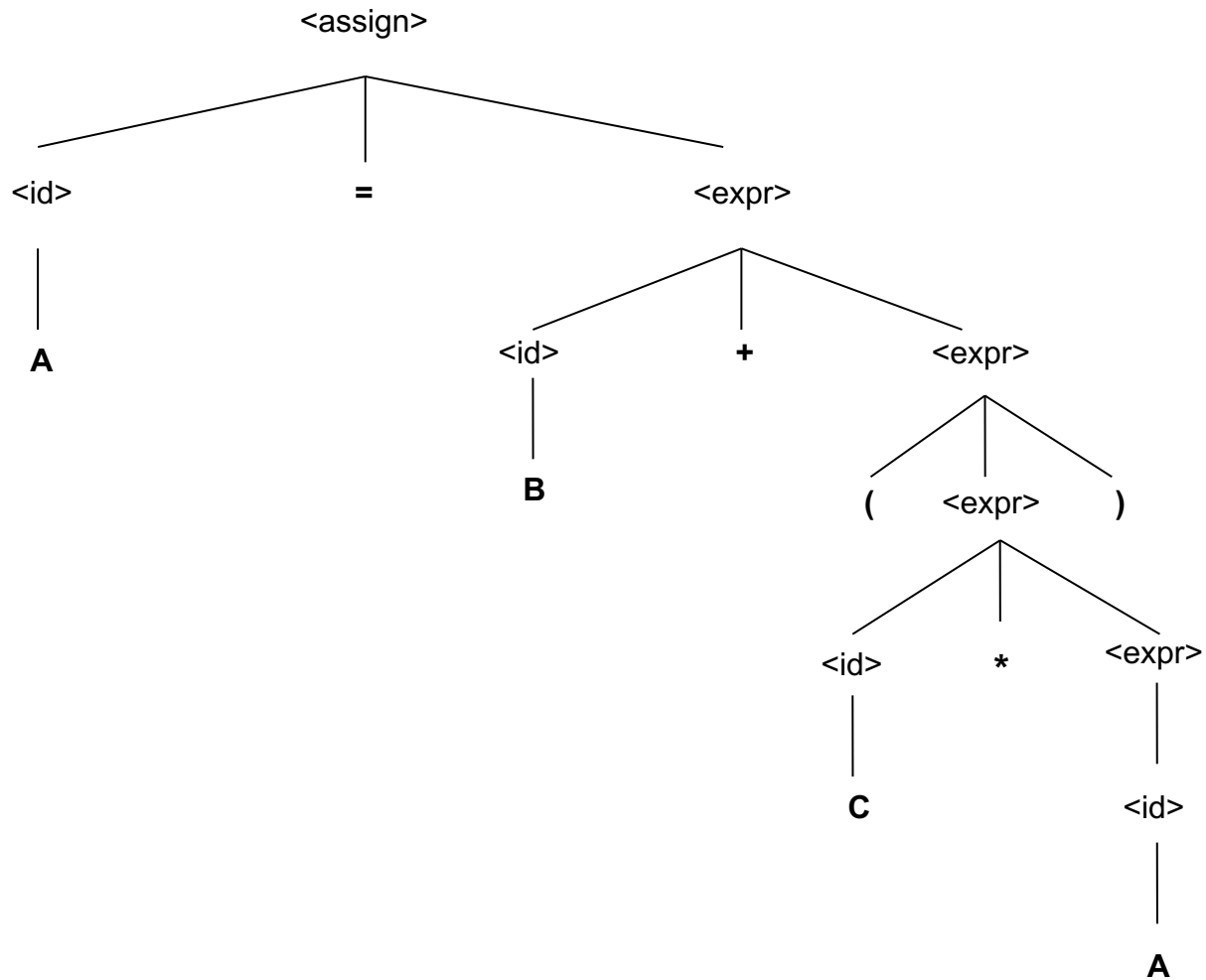
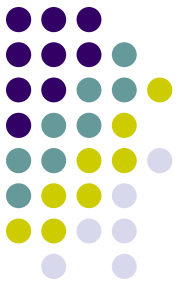
$\Rightarrow A = B + ( \langle \text{id} \rangle * \langle \text{expr} \rangle )$

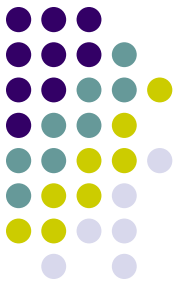
$\Rightarrow A = B + ( C * \langle \text{expr} \rangle )$

$\Rightarrow A = B + ( C * \langle \text{id} \rangle )$

$\Rightarrow A = B + ( C * A )$

# Parse tree for $A = B + (C * A)$





# BNF Grammar (Example 2)

- $T = \{=, A, B, C, +, *, (, )\}$
- $N = \{\langle\text{assign}\rangle, \langle\text{id}\rangle, \langle\text{expr}\rangle\}$
- $S = \langle\text{assign}\rangle$
- $P = \{$

$\langle\text{assign}\rangle \rightarrow \langle\text{id}\rangle = \langle\text{expr}\rangle$

$\langle\text{id}\rangle \rightarrow A \mid B \mid C$

$\langle\text{expr}\rangle \rightarrow \langle\text{expr}\rangle + \langle\text{expr}\rangle$

$\mid \langle\text{expr}\rangle * \langle\text{expr}\rangle$

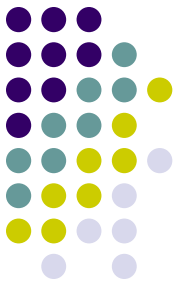
$\mid ( \langle\text{expr}\rangle )$

$\mid \langle\text{id}\rangle$

$\}$

- Derivation for  $A = B + C * A$  ?

# One Possible Derivation



<assign>

=> <id> = <expr>

=> A = <expr> + <expr>

=> A = <id> + <expr>

=> A = B + <expr>

=> A = B + <expr> \* <expr>

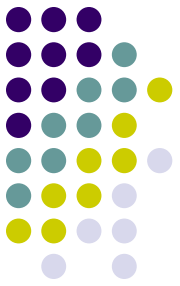
=> A = B + <id> \* <expr>

=> A = B + C \* <expr>

=> A = B + C \* <id>

=> A = B + C \* A

# The Other Possible Derivation



<assign>

$\Rightarrow$  <id> = <expr>

$\Rightarrow$  A = <expr>

$\Rightarrow$  A = <expr> \* <expr>

$\Rightarrow$  A = <expr> + <expr> \* <expr>

$\Rightarrow$  A = <id> + <expr> \* <expr>

$\Rightarrow$  A = B + <expr> \* <expr>

$\Rightarrow$  A = B + <id> \* <expr>

$\Rightarrow$  A = B + C \* <expr>

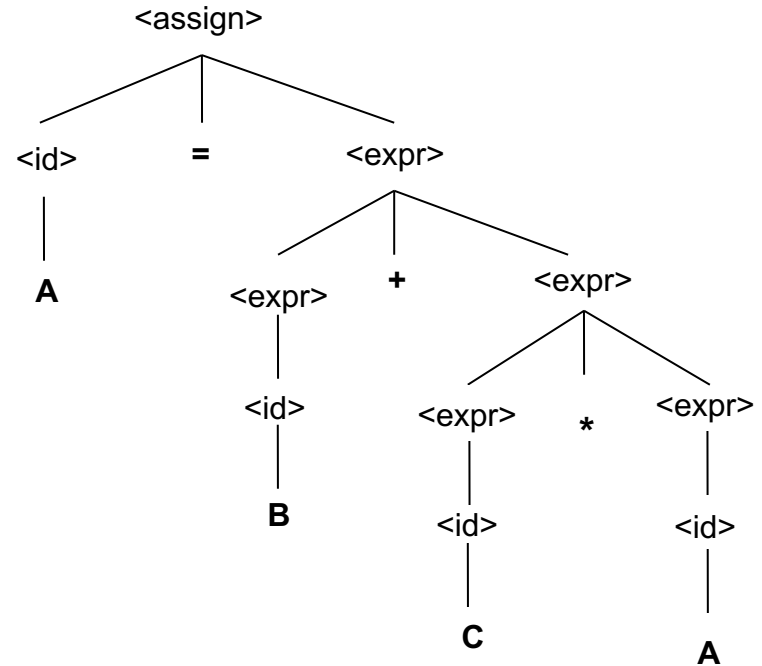
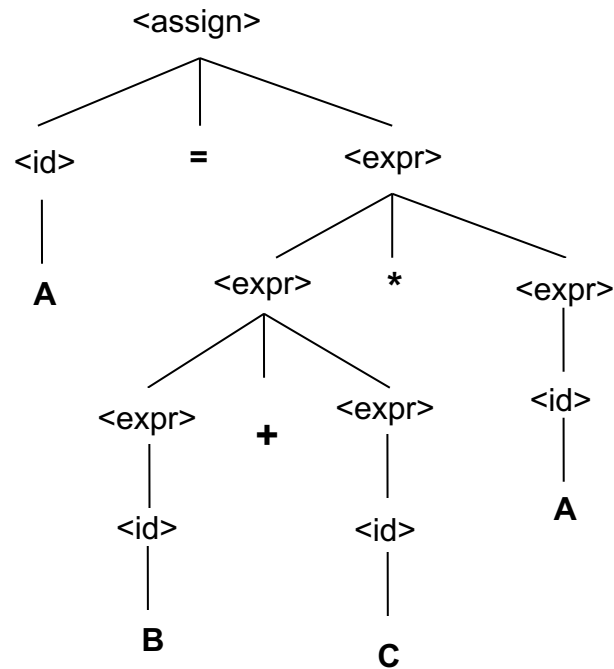
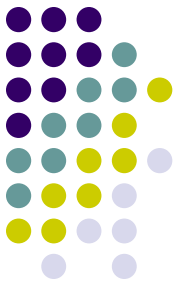
$\Rightarrow$  A = B + C \* <id>

$\Rightarrow$  A = B + C \* A

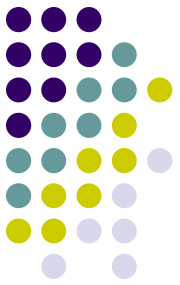


# Example 2

## Parse Trees for $A = B + C * A$



- Ambiguous

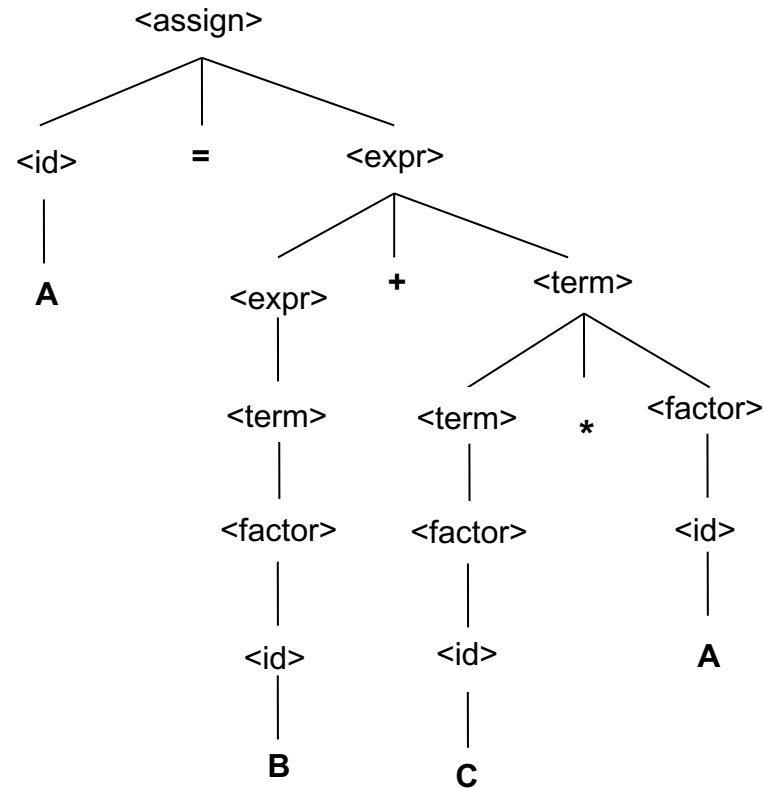
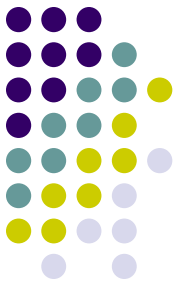


# BNF Grammar (Example 3)

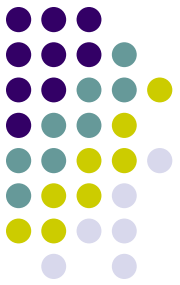
- $T = \{=, A, B, C, +, *, (, )\}$
- $N = \{\langle \text{assign} \rangle, \langle \text{id} \rangle, \langle \text{expr} \rangle, \langle \text{term} \rangle, \langle \text{factor} \rangle\}$
- $S = \langle \text{assign} \rangle$
- $P = \{$ 
  - $\langle \text{assign} \rangle \rightarrow \langle \text{id} \rangle = \langle \text{expr} \rangle$
  - $\langle \text{id} \rangle \rightarrow A \mid B \mid C$
  - $\langle \text{expr} \rangle \rightarrow \langle \text{expr} \rangle + \langle \text{term} \rangle \mid \langle \text{term} \rangle$
  - $\langle \text{term} \rangle \rightarrow \langle \text{term} \rangle * \langle \text{factor} \rangle \mid \langle \text{factor} \rangle$
  - $\langle \text{factor} \rangle \rightarrow ( \langle \text{expr} \rangle ) \mid \langle \text{id} \rangle$ $\}$
- Parse tree for  $A = B + C * A$  ?

# Example 3

## Parse Tree for $A = B + C * A$



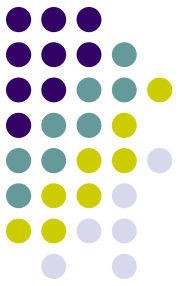
- Operator precedence



# Parsing

- Top Down
  - Recursive Descent
  - LL Parsing – Left to right scan of the input; Leftmost derivation
- Bottom Up
  - Shift Reduce
  - LR Parsing – Left to right scan of the input; Rightmost derivation

# LL(1) Grammar for a Small Programming Language



$T = \{\text{begin, end, ;, =, A, B, C, +, *}\}$

$N = \{\langle \text{program} \rangle, \langle \text{stmt\_list} \rangle, \langle \text{stmt} \rangle, \langle \text{var} \rangle, \langle \text{stmt\_tail} \rangle, \langle \text{expression} \rangle, \langle \text{expr\_tail} \rangle\}$

Start =  $\langle \text{program} \rangle$

P =

- {
- 1.  $\langle \text{program} \rangle \rightarrow \text{begin } \langle \text{stmt\_list} \rangle \text{ end}$
- 2.  $\langle \text{stmt\_list} \rangle \rightarrow \langle \text{stmt} \rangle \langle \text{stmt\_tail} \rangle$
- 3.  $\langle \text{stmt\_tail} \rangle \rightarrow ; \langle \text{stmt\_list} \rangle$
- 4.  $\langle \text{stmt\_tail} \rangle \rightarrow \lambda$
- 5.  $\langle \text{stmt} \rangle \rightarrow \langle \text{var} \rangle = \langle \text{expression} \rangle$
- 6.  $\langle \text{var} \rangle \rightarrow \mathbf{A}$
- 7.  $\langle \text{var} \rangle \rightarrow \mathbf{B}$
- 8.  $\langle \text{var} \rangle \rightarrow \mathbf{C}$
- 9.  $\langle \text{expression} \rangle \rightarrow \langle \text{var} \rangle \langle \text{expr\_tail} \rangle$
- 10.  $\langle \text{expr\_tail} \rangle \rightarrow + \langle \text{var} \rangle \langle \text{expr\_tail} \rangle$
- 11.  $\langle \text{expr\_tail} \rangle \rightarrow * \langle \text{var} \rangle \langle \text{expr\_tail} \rangle$
- 12.  $\langle \text{expr\_tail} \rangle \rightarrow \lambda$
- }

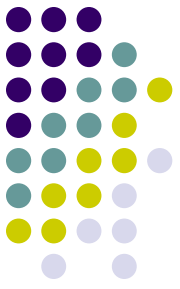
Example 1:

```
begin
    A = B + C;
    C = A * B
end
```

Example 2:

```
begin
    A = B + A * C;
    C = A * B;
end
```

# Parsing of Example 1



From main parsing routine, call <program> function

From <program>, match **begin**; call <stmt\_list> function

From <stmt\_list>, see **A** call <stmt> function

From <stmt>, see **A** call <var> function

From <var>, match **A**; return

From <stmt>, match =; see **B** call <expression> function

From <expression>, see **B** call <var> function

From <var>, match **B**; return

From <expression>, see + call <expr\_tail> function

From <expr\_tail>, match +; see **C** call <var> function

From <var>, match **C**; return

From <expr\_tail>, see ; call <expr\_tail>

From <expr\_tail>, see ; return

From <expr\_tail>, return

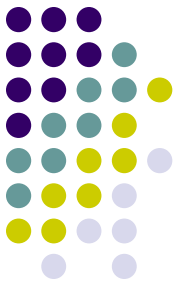
From <expression>, return

...

From <program>, match end; return

From main parsing routine, print error count and terminate

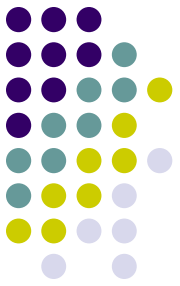
# Recursive Descent Parser for a Small Programming Language



1) `<program>` → **begin** `<stmt_list>` **end**

```
program ()
{
    if (current_token == begin)
    { // rule 1
        get_next_token;
        call stmt_list;
        if (current_token == end)
            get_next_token;
        else
            call error_routine;
    }
    else
        call error_routine;
    return;
}
```

# Recursive Descent Parser for a Small Programming Language

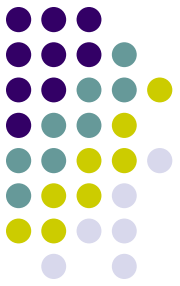


2)  $\langle \text{stmt\_list} \rangle \rightarrow \langle \text{stmt} \rangle \langle \text{stmt\_tail} \rangle$

```
stmt_list ()
{ // rule 2
    call stmt;
    call stmt_tail;
    return;
}
```



# Recursive Descent Parser for a Small Programming Language

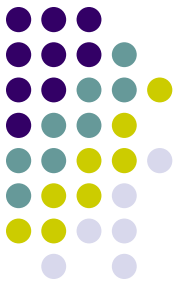


3)  $\langle \text{stmt\_tail} \rangle \rightarrow ; \langle \text{stmt\_list} \rangle$

4)  $\langle \text{stmt\_tail} \rangle \rightarrow \lambda$

```
stmt_tail ()
{
    if (current_token == ;)
    { // rule 3
        get_next_token;
        call stmt_list;
    }
    else if (current_token == end)
    { // rule 4
    }
    else
        call error_routine;
    return;
}
```

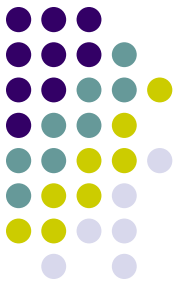
# Recursive Descent Parser for a Small Programming Language



5) `<stmt> → <var> = <expression>`

```
stmt ()
{ // rule 5
  call var;
  if (current_token == =)
  {
    get_next_token;
    call expression;
  }
  else
    call error_routine;
  return;
}
```

# Recursive Descent Parser for a Small Programming Language



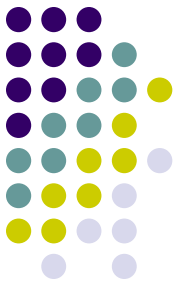
6) <var> → A

7) <var> → B

8) <var> → C

```
var ()
{ // rule 5
    if (current_token == A)
    { // rule 6
        get_next_token;
    }
    else if (current_token == B)
    { // rule 7
        get_next_token;
    }
    else if (current_token == C)
    { // rule 8
        get_next_token;
    }
    else
        call error_routine;
    return;
}
```

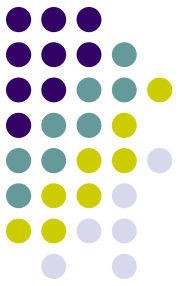
# Recursive Descent Parser for a Small Programming Language



9)  $\langle \text{expression} \rangle \rightarrow \langle \text{var} \rangle \langle \text{expr\_tail} \rangle$

```
expression ()
{ // rule 9
    call var;
    call expr_tail;
    return;
}
```

# Recursive Descent Parser for a Small Programming Language

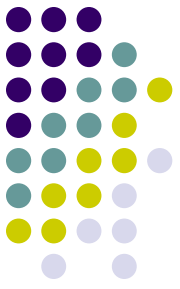


- 10) `<expr_tail> → + <var><expr_tail>`
- 11) `<expr_tail> → * <var><expr_tail>`
- 12) `<expr_tail> → λ`

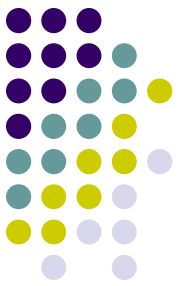
```
expr_tail ()
{
    if (current_token == +)
    { // rule 10
        get_next_token;
        call var;
        call expr_tail;
    }
    else if (current_token == *)
    { // rule 11
        get_next_token;
        call var;
        call expr_tail;
    }
    else if (current_token == ; or current_token == end)
    { // rule 12
    }
    else
        call error_routine;
    return;
}
```

# Context Free Grammar

## Definition



- Given a Context Free Grammar of the form:
  - Terminals =  $\{T_1, T_2, T_3, \dots\}$
  - Non-terminals =  $\{\langle nt_1 \rangle, \langle nt_2 \rangle, \langle nt_3 \rangle, \dots\}$
  - A Start symbol from the set of non-terminals
  - A set of Production rules of the form  
 $\langle nt_i \rangle \rightarrow$  string of T and  $\langle nt \rangle$  symbols



# First and Follow Sets

- **Firsts**
  - A terminal symbol  $T_i$  is a member of the First Set of non-terminal symbol  $\langle nt_j \rangle$  if  $T_i$  can become the first terminal symbol in a complete expansion of  $\langle nt_j \rangle$ .
- **Follows**
  - A terminal symbol  $T_i$  is a member of the Follow Set of non-terminal symbol  $\langle nt_j \rangle$  if  $T_i$  can become the first terminal symbol immediately following a complete expansion of  $\langle nt_j \rangle$ .